



Vardanega, P. J., & Bolton, M. (2016). Discussion of “Characterization of Model Uncertainty for Cantilever Deflections in Undrained Clay” by D. M. Zhang, K. K. Phoon, H. W. Huang, and Q. F. Hu. *Journal of Geotechnical and Geoenvironmental Engineering*, 142(1), [07015036]. [https://doi.org/10.1061/\(ASCE\)GT.1943-5606.0001395](https://doi.org/10.1061/(ASCE)GT.1943-5606.0001395)

Peer reviewed version

Link to published version (if available):  
[10.1061/\(ASCE\)GT.1943-5606.0001395](https://doi.org/10.1061/(ASCE)GT.1943-5606.0001395)

[Link to publication record in Explore Bristol Research](#)  
PDF-document

Vardanega, P., & Bolton, M. (2015). Discussion of “Characterization of Model Uncertainty for Cantilever Deflections in Undrained Clay” by D. M. Zhang, K. K. Phoon, H. W. Huang, and Q. F. Hu. *Journal of Geotechnical and Geoenvironmental Engineering*, [07015036]. [http://dx.doi.org/10.1061/\(ASCE\)GT.1943-5606.0001395](http://dx.doi.org/10.1061/(ASCE)GT.1943-5606.0001395). This material may be downloaded for personal use only. Any other use requires prior permission of the American Society of Civil Engineers.

## University of Bristol - Explore Bristol Research

### General rights

This document is made available in accordance with publisher policies. Please cite only the published version using the reference above. Full terms of use are available:  
<http://www.bristol.ac.uk/red/research-policy/pure/user-guides/ebr-terms/>

This is the final draft of a manuscript that was accepted for publication in the *Journal of Geotechnical and Geoenvironmental Engineering* (American Society of Civil Engineers) on 30 March 2015. [The original line numbering has been removed and a watermark added].

Alterations to this final draft may have been introduced during the publishing process, such as: formatting changes and resolution of typographical errors.

For the version of record please refer to the final published version at:

[http://dx.doi.org/10.1061/\(ASCE\)GT.1943-5606.0001395](http://dx.doi.org/10.1061/(ASCE)GT.1943-5606.0001395)

PJV

21-08-2015

Discussion of “Characterization of Model Uncertainty for Cantilever Deflections in Undrained Clay” by D. M. Zhang, K. K. Phoon, H. W. Huang and Q. F. Hu

[http://dx.doi.org/10.1061/\(ASCE\)GT.1943-5606.0001205](http://dx.doi.org/10.1061/(ASCE)GT.1943-5606.0001205)

P. J. Vardanega, Ph.D. M.ASCE<sup>1</sup> and M. D. Bolton, Ph.D. C.Eng.<sup>2</sup>

## Introduction

The authors have presented an interesting and welcome study of cantilever wall displacements due to the excavation of soil, first relating simplified Mobilized Strength Design (MSD) calculations (Osman and Bolton 2004, 2006) to more complex Finite Element Analyses (FEA) of a range of excavation geometries and wall stiffnesses, and then linking MSD principles to the probabilistic assessment of soil and model parameters. The calibration of MSD against FEA is welcome because it extends the earlier work of Osman and Bolton (2004), and does so in a rigorous fashion. Putting these calibrated MSD estimates into the framework of reliability, by allowing for uncertainty in the estimates of system parameters, is also welcome because it enables probabilistic decision-makers to focus on more realistic definitions of the failures they are seeking to avoid. The transition from notional concepts of ultimate failure, based on the statistics of peak strength, towards the statistical assessment of ground movements and their possible consequences, also requires an understanding of additional parametric uncertainties (e.g. Phoon and Kulhawy 1999). We agree with the authors that, to be practical, such assessments need to be made on the basis of simplified

---

<sup>1</sup> Lecturer in Civil Engineering, Department of Civil Engineering, University of Bristol, Bristol, BS8 1TR, United Kingdom. Email: [p.j.vardanega@bristol.ac.uk](mailto:p.j.vardanega@bristol.ac.uk) (corresponding author)

<sup>2</sup> Professor of Soil Mechanics, Department of Engineering, University of Cambridge, Cambridge, CP2 1PZ, United Kingdom. Email: [mdb8@cam.ac.uk](mailto:mdb8@cam.ac.uk)

behavioural models and the simplest possible constitutive relations. We have some further comments that draw upon recently published work of the discussers.

### **Soil Stiffness Degradation**

While the apparent accuracy of the finite element back-calculations of cantilever wall displacements in Figure 10 is excellent, they must be dependent on the HSSmall parameters, namely the shear modulus at very small strains ( $G_0$ ), the elastic modulus at very small strains ( $E_0$ ), the shear strain required to reduce  $G/G_0$  to 0.7 ( $\gamma_{0.7}$ ) and the asymptotic value of the deviatoric stress ( $q_a$ ) introduced in equation 8. However, the authors' database of field case studies in Appendix II only lists an unload-reload modulus ( $E_{ur}$ ), but does not precisely specify the strain magnitude at which it was determined. Could the authors offer further information?

The accuracy of their recalibrated displacement predictions compared with centrifuge test results, as shown by the authors in Figure 13, is also remarkable. However, this excellence of fit must surely also be regarded as fortuitous considering the apparently subjective definition chosen for the unload-reload modulus ( $E_{ur}$ ), the assumption of a constant ratio  $E/s_u$ , the undeclared and uncertain relationship between  $E_{ur}$  and the parameters  $G_0$  and  $q_a$  set out in equation 8, and the universal assumption of the quoted value of  $\gamma_{0.7}$ .

While these potential drawbacks inevitably introduce uncertainties and errors into the prediction of real wall displacements made using the authors' approach to the HSSmall soil model, they need not be taken to detract from the authors' calibration of MSD against FEA (via regression function  $f$  in equations 7 and 10) which use the same soil model in each case.

The established consensus is that the shear stiffness  $G_0$  at very small strains should be measured, and must be understood to vary in service with the square root of mean effective stress. The shear stress at small to moderate strains can then best be estimated on the

assumption of a quasi-hyperbolic stress-strain curve, conventionally normalised using the strain  $\gamma_{ref}$  which is found to reduce  $G/G_0$  to 0.5. Darendeli (2001), Zhang et al. (2005) and Vardanega and Bolton (2013, 2014) present databases that offer statistical correlations against routine characterisation information such as the Atterberg Limits (and in the case of Vardanega and Bolton 2013, 2014 an allowance for relevant rate effects), enabling a prior fit to be obtained against the published stiffness reduction data of fine grained materials even before project-specific data becomes available.

A new approach for fine-grained soils does not rely on the measurement of  $G_0$  but instead bases the non-linear stress-strain relation on knowledge of the undrained shear strength ( $s_u$ ) and the measurement of the strain ( $\gamma_{M=2}$ ) required to mobilise half of it. Vardanega and Bolton (2011, 2012) have shown that a power curve of normalised shear stress  $\tau/s_u$  versus normalised shear strain  $\gamma/\gamma_{M=2}$  raised to the power  $b$ , enables adequate strain predictions to be made for  $\tau/s_u$  between 0.2 and 0.8 for 19 natural clays with widely varying characteristics. Furthermore, Vardanega et al. (2012) show evidence of the variation of  $\gamma_{M=2}$  and  $b$  with overconsolidation ratio for a particular reconstituted kaolin. Some prior evidence therefore exists on the expected ranges within which project-specific parameter values should fall. The final establishment of satisfactory design values for the curve-fitting parameters  $s_u$ ,  $\gamma_{M=2}$  and  $b$  requires only competent triaxial tests on cores tested with an accuracy on strain of at least 0.02%, or equivalent pressuremeter tests in the field. Engineers may then conduct their own deterministic calculations of displacement with parameters chosen from a range of depth profiles for each of  $s_u$ ,  $\gamma_{M=2}$  and  $b$ .

### **Dimensionless Groups for Deep Excavations**

The authors make a good finding of the regression function  $f$  between simplified MSD estimates of wall crest displacement and FEA estimates, related to six dimensionless groups

namely, normalised excavation depth ( $H/D$ ), normalised excavation width ( $B/2D$ ), relative wall stiffness ( $\gamma D^4/EI$ ), earth pressure coefficient ( $K_0$ ), strength ratio ( $s_u/\sigma'_v$ ) and stiffness ratio ( $E_{ur}/S_u$ ). Two other groups may be worth studying in a similar fashion, in relation to the bulging of a braced wall below the level of the lowest installed prop. This mode of deformation usually leads to the greatest displacements, which occur below dredge level, creating a corresponding settlement trough in the retained ground. Therefore, bulging is usually critical in structural serviceability checks both for the retaining wall itself and any structure that rests on the retained ground.

Lam and Bolton (2011) and Lam et al. (2014) demonstrated some success in predicting the peak bulging displacement ( $w_{max}$ ) using an energy balance for a MSD deformation mechanism based on the assumption of a sinusoidal bulge of wavelength ( $\lambda$ ). Bolton et al. (2014) have recently published a follow-up study of excavations in Shanghai, analysing and extending the database of Xu (2007), and making use of the power law soil model introduced above. In this study a new dimensionless group is introduced in equation 1 to improve upon the system stiffness definition of Clough et al. (1989) which involved the prop spacing interval. A modified system stiffness,  $\eta^*$  (not to be confused with the residual random part of the MSD calibration, also denoted  $\eta^*$  in the original paper) was defined:

$$\eta^* = \frac{EI}{\gamma_w \lambda^4} \quad (1)$$

This has the logical advantage of relating the wall flexural stiffness ( $EI$ ) to the unsupported length ( $\lambda$ ) of the bulging portion of the wall.

The bulge amplitude  $w_{max}$  was then expressed as a normalised shear strain in the retained ground, using the definition of modified mobilisation parameter  $\psi^*$  (expressed in terms of the mobilisation factor,  $M$  and  $b$  in equation 2)

$$\psi^* = \frac{2w_{max}}{\lambda_{average} \gamma M=2} = \left(\frac{2}{M}\right)^{1/b} \quad (2)$$

It was shown that field monitoring data mapped well on plots of  $\psi^*$  versus  $\eta^*$  when the range of soil strength profiles and excavation depths was allowed for. It would be interesting to see if  $\eta^*$  and  $\psi^*$  are also significant in an assessment of the correction factor  $\eta$  via  $f$  using the database presented in the paper under discussion, where wavelength  $\lambda$  would be replaced by wall depth  $D$  in the cantilever phase.

### Notation

*The following symbols are used in this paper:*

$b$  = an exponent

$B$  = excavation width

$D$  = wall depth

$E$  = elastic modulus

$EI$  = wall flexural stiffness

$E_0$  = elastic modulus at very small strains

$E_{ur}$  = unload-reload modulus

$f$  = a regression function

$G$  = shear modulus

$G_0$  = shear modulus at very small strains

$H_c$  = excavation depth

$K_0$  = earth pressure coefficient

$M$  = mobilization factor

$q_a$  = asymptotic value of the deviatoric stress

$s_u$  = undrained shear strength

$w_{max}$  = maximum wall bulge

$\gamma$  = shear strain (or unit weight of soil when calculating relative wall stiffness)

$\gamma_{0.7}$  = shear strain required to reduce  $G/G_0$  to 0.7

$\gamma_{M=2}$  = shear strain to mobilize  $0.5s_u$

$\gamma_{ref}$  = shear strain required to reduce  $G/G_0$  to 0.5

$\gamma_w$  = unit weight of water

$\eta^*$  = modified system stiffness

$\lambda$  = wavelength

$\sigma'_v$  = vertical effective stress

$\tau$  = mobilized shear stress

$\psi^*$  = modified mobilisation parameter

## References

- Bolton, M. D., Lam, S.-Y., Vardanega, P. J., Ng, C. W. W. and Ma, X. (2014). Ground Movements due to deep excavations in Shanghai: Design charts. *Frontiers of Structural and Civil Engineering*, **8(3)**: 201-236, <http://dx.doi.org/10.1007/s11709-014-0253-y>
- Clough G. W., Smith E. W., Sweeney, B. P. (1989). Movement control of excavation support systems by iterative design. *Foundation engineering current principles and practice* (American Society of Civil Engineers), New York, 1989, **2**: 869–884.
- Darendeli, M. B. (2001). *Development of a new family of normalized modulus reduction and material damping curves*. Ph.D. thesis, University of Texas at Austin.
- Lam, S.Y., Bolton, M.D. (2011). Energy conservation as a principle underlying mobilizable strength design for deep excavations. *Journal of Geotechnical and Geoenvironmental Engineering* **137(11)**: 1062-1074. [http://dx.doi.org/10.1061/\(ASCE\)GT.1943-5606.0000510](http://dx.doi.org/10.1061/(ASCE)GT.1943-5606.0000510)



- Lam, S. Y., Haigh, S. K. and Bolton, M. D. (2014). Understanding ground deformation mechanisms for multi-propped excavation in soft clay. *Soils and Foundations*, **54(3)**: 296-312. <http://dx.doi.org/10.1016/j.sandf.2014.04.005>
- Osman, A. S. and Bolton, M. D. (2004). A new design method for retaining walls in clay. *Canadian Geotechnical Journal*, **41(3)**: 451-466. <http://dx.doi.org/10.1139/t04-003>
- Osman, A. S. and Bolton, M. D. (2006). Ground movement predictions for braced excavations in undrained clay. *Journal of Geotechnical and Geoenvironmental Engineering*, **132(4)**: 465- 477. [http://dx.doi.org/10.1061/\(ASCE\)1090-0241\(2006\)132:4\(465\)](http://dx.doi.org/10.1061/(ASCE)1090-0241(2006)132:4(465))
- Phoon, K. and Kulhawy, F. H. (1999). Characterisation of geotechnical variability. *Canadian Geotechnical Journal*, **36(4)**: 612-624. <http://dx.doi.org/10.1139/t99-038>
- Vardanega, P.J. and Bolton, M.D. (2011) Strength mobilization in clays and silts. *Canadian Geotechnical Journal* **48(10)**: 1485-1503, <http://dx.doi.org/10.1139/t11-052>
- Vardanega, P. J., and Bolton, M.D. (2012). “Corrigendum: Strength mobilization in clays and silts.” *Canadian Geotechnical Journal* **49(5)**: 631. <http://dx.doi.org/10.1139/t2012-023>
- Vardanega, P.J., Lau, B.H., Lam, S.Y., Haigh, S.K., Madabhushi S.P.G. and Bolton, M.D. (2012). Laboratory measurement of strength mobilisation in kaolin: link to stress history. *Géotechnique Letters*, **2(1)**: 9-15. <http://dx.doi.org/10.1680/geolett.12.00003>
- Vardanega, P. J. and Bolton, M. D. (2013). Stiffness of Clays and Silts: Normalizing Shear Modulus and Shear Strain. *Journal of Geotechnical and Geoenvironmental Engineering*, **139(9)**: 1575-1589. [http://dx.doi.org/10.1061/\(ASCE\)GT.1943-5606.0000887](http://dx.doi.org/10.1061/(ASCE)GT.1943-5606.0000887)
- Vardanega, P. J. and Bolton, M. D. (2014). Stiffness of Clays and Silts: Modeling Considerations. *Journal of Geotechnical and Geoenvironmental Engineering*, **140(6)**: 06014004. [http://dx.doi.org/10.1061/\(ASCE\)GT.1943-5606.0001104](http://dx.doi.org/10.1061/(ASCE)GT.1943-5606.0001104)

- Xu, Z. H. (2007). *Deformation behaviour of deep excavations supported by permanent structure in Shanghai soft deposit*. Ph.D. thesis. Shanghai: Shanghai Jiao Tong University, Shanghai, China (in Chinese).
- Zhang, J., Andrus, R. D. and Juang, C. H. (2005). Normalised Shear Modulus and Material Damping Ratio Relationships. *Journal of Geotechnical and Geoenvironmental Engineering*, **131(4)**: 453-464. [http://dx.doi.org/10.1061/\(ASCE\)1090-0241\(2005\)131:4\(453\)](http://dx.doi.org/10.1061/(ASCE)1090-0241(2005)131:4(453))
- Zhang, D. M., Phoon, K. K., Huang, H. W. and Fu, Q. F. (2015). Characterisation of Model Uncertainty for Cantilever Deflections in Undrained Clay. *Journal of Geotechnical and Geoenvironmental Engineering*, **141(1)**: 04014088. [http://dx.doi.org/10.1061/\(ASCE\)GT.1943-5606.0001205](http://dx.doi.org/10.1061/(ASCE)GT.1943-5606.0001205)